## UNIT 2 • REASONING WITH LINEAR EQUATIONS AND INEQUALITIES

## Guided Practice 2.9.1

## Example 1

What is the fourth term of the sequence given by the formula $a_{n}=a_{n-1}+5$, where $a_{n}$ is the value of the term, $n$ is the term number, and $a_{1}=2$ ?

1. Determine whether the sequence is explicit or recursive.

The formula defines a term in the sequence, $a_{n}$, with regard to the term before it, $a_{n-1}$. Therefore, this is a recursive sequence.
2. Use the given formula to find the first 4 terms of the sequence.

The first term of the sequence is given: $a_{1}=2$.
Use this term to find the second term in the sequence.

$$
\begin{array}{ll}
a_{n}=a_{n-1}+5 & \text { Given formula } \\
a_{2}=a_{2-1}+5 & \text { Substitute } 2 \text { for } n . \\
a_{2}=a_{1}+5 & \text { Simplify the subscript. } \\
a_{2}=(2)+5 & \text { Substitute } 2 \text { for } a_{1} . \\
a_{2}=7 & \text { Simplify. }
\end{array}
$$

The second term of the sequence is 7 .
Use this term to find the third term in the sequence.

$$
\begin{array}{ll}
a_{n}=a_{n-1}+5 & \text { Given formula } \\
a_{3}=a_{3-1}+5 & \text { Substitute } 3 \text { for } n . \\
a_{3}=a_{2}+5 & \text { Simplify the subscript. } \\
a_{3}=(7)+5 & \text { Substitute } 7 \text { for } a_{2} . \\
a_{3}=12 & \text { Simplify. }
\end{array}
$$

The third term of the sequence is 12 .
Use this term to find the fourth term in the sequence.

$$
\begin{array}{ll}
a_{n}=a_{n-1}+5 & \text { Given formula } \\
a_{4}=a_{4-1}+5 & \text { Substitute } 4 \text { for } n . \\
a_{4}=a_{3}+5 & \text { Simplify the subscript. } \\
a_{4}=(12)+5 & \text { Substitute } 12 \text { for } a_{3} . \\
a_{4}=17 & \text { Simplify. }
\end{array}
$$

The fourth term of the sequence is 17 .

## UNIT 2 • REASONING WITH LINEAR EQUATIONS AND INEQUALITIES

## Example 2

Identify the missing terms in the sequence using recursion.

$$
A=\left\{8,13,18,23, a_{5}, a_{6}, a_{7}\right\}
$$

1. Determine the pattern by looking for a common difference. Use this information to write a formula to find $a_{n}$.

Subtract the first term from the second term and then continue that pattern to see if the difference between each pair of terms is the same.

$$
\begin{aligned}
& a_{2}-a_{1}=13-8=5 \\
& a_{3}-a_{2}=18-13=5 \\
& a_{4}-a_{3}=23-18=5
\end{aligned}
$$

The terms are separated by a common difference of 5 . This means that to find each term $\left(a_{n}\right)$, add 5 to the term before it $\left(a_{n-1}\right)$.

From this, we can deduce that $a_{n}=a_{n-1}+5$.
2. Use the formula to find the missing terms.

Find each missing term, $a_{n}$, by substituting the term immediately before it for $a_{n-1}$ and solving for $a_{n}$.

The missing terms are $a_{5}, a_{6}$, and $a_{7}$.

$$
\begin{aligned}
& a_{n}=a_{n-1}+5 \\
& a_{5}=a_{4}+5=23+5=28 \\
& a_{6}=a_{5}+5=28+5=33 \\
& a_{7}=a_{6}+5=33+5=38
\end{aligned}
$$

The missing terms are 28,33 , and 38 .

## UNIT 2 • REASONING WITH LIINEAR EQUATIONS AND INEQUALITIES

## Instruction

## Example 3

Find the ninth term in the sequence given by the formula $a_{n}=3 n+1$, where $a_{n}$ is the value of the term and $n$ is the term number. Then, find and graph the first 5 terms in the sequence.

1. Determine whether this is an explicit formula or a recursive formula, then use the formula to find the desired term.

The formula is explicit because plugging in the given term number (9 in this case) will produce the desired term. Substitute 9 for $n$ and solve.

$$
\begin{array}{ll}
a_{n}=3 n+1 & \text { Given formula } \\
a_{9}=3(9)+1 & \\
a_{9}=27+1 & \text { Substitute } 9 \text { for } n . \\
a_{9}=28 & \text { Multiply. } \\
\text { Add. }
\end{array}
$$

The ninth term in the sequence is 28 .
2. Find the first 5 terms of the sequence.

Substitute $1,2,3,4$, and 5 , respectively, for $n$, then solve for the term.

$$
\begin{aligned}
& a_{n}=3 n+1 \\
& a_{1}=3(1)+1=4 \\
& a_{2}=3(2)+1=7 \\
& a_{3}=3(3)+1=10 \\
& a_{4}=3(4)+1=13 \\
& a_{5}=3(5)+1=16
\end{aligned}
$$

The first 5 terms are $4,7,10,13$, and 16 .

## UNIT 2 • REASONING WITH LINEAR EQUATIONS AND INEQUALITIES Lesson 9: Sequences As Functions

3. Create ordered pairs from the sequence. $n$ is the first coordinate, and $a_{n}$ is the second coordinate.
( $n, a_{n}$ )
$(1,4)$
$(2,7)$
$(3,10)$
$(4,13)$
$(5,16)$
4. Plot the ordered pairs.

| $\boldsymbol{a}_{\boldsymbol{n}} \mathbf{4}$ |  |  |  |  |  |  |  |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 18 |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |
| 15 |  |  |  |  |  |  |  |
| 14 |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |
| 1 |  |  |  |  |  |  |  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | $\boldsymbol{n}$ |

