## Lesson 2: Working with Two Variables

## Prerequisite Skills

This lesson requires the use of the following skills:

- creating tables with multiple rows and columns (no standard)
- reading tables with multiple rows and columns (no standard)


## Introduction

When data compares characteristics of two or more categories, the data can be displayed in a two-way frequency table. In this lesson, we focus on two-way frequency tables that compare survey results. When used to analyze survey results, a two-way frequency table is a table of data that separates responses by a characteristic of the respondents.

| Type of characteristic | Type of response |  |
| :--- | :---: | :---: |
|  | Response 1 | Response 2 |
| Characteristic 1 | $a$ | $b$ |
| Characteristic 2 | $c$ | $d$ |

Each cell in the table contains a count of the people with a given characteristic who gave each response. For example, in this table, $a, b, c$, and $d$ would each represent the number of responses given by people with each characteristic. That is, $a$ represents people with Characteristic 1 who gave Response $1, b$ represents people with Characteristic 1 who gave Response 2, and so on. The sum of all the cells, $a+b+c+d$, is the total number of respondents. Two-way frequency tables help organize information and provide greater insight into features of a population being surveyed. A trend, or pattern in the data, can be examined using a two-way frequency table.

A joint frequency is the number of times a pair of characteristics appear together. The entries in the cells of a two-way frequency table are joint frequencies. In the sample table, $a, b, c$, and $d$ are each a joint frequency. A marginal frequency is the total number of times a characteristic occurs. This is the sum of either a row or a column in a two-way frequency table. In the sample table, $a+b$ would be the marginal frequency of people with Characteristic 1.

A conditional relative frequency allows a comparison to be made between a joint frequency and the total number of responses in a single row, a single column, or the entire table. Relative frequencies are usually expressed as a decimal. They are found by dividing the number of responses by either the total number of people who gave that response, the total number of people with a given characteristic, or the total number of respondents. In the sample table, $\frac{a}{a+b}$ is the relative frequency of Response 1 for people with Characteristic 1.

## UNIT $6 \cdot$ DESCRIBING DATA

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## Instruction

## Key Concepts

- A two-way frequency table divides survey responses by characteristics of respondents.
- The number of times a response was given by people with a certain characteristic is called a joint frequency.
- A marginal frequency is the total number of times a response is given, or the total number of people with a certain characteristic.
- A conditional relative frequency is usually written as a decimal. It expresses a number of responses divided by the total number of respondents, the total number of people with a given characteristic, or the total number of times a specific response was given.
- Trends, or patterns of responses, can be identified by looking at the frequency of responses.


## Common Errors/Misconceptions

- incorrectly locating frequencies in the table
- incorrectly calculating conditional relative frequencies by being inconsistent in the method used (dividing by the number of times a response was given, the number of people with a given characteristic, or the total number of respondents)

